Math 4326 Dr. Duval

LINEAR ALGEBRA Homework

Monday, April 27

Follow the separate general guidelines for Parts A,B,C. Be sure to include and label *all* four standard parts (a), (b), (c), (d) of Part A in what you hand in.

Characteristic and Minimal Polynomials (Part II)

Section 8.C, pp. 264–267

A: Reading questions. Due by 2pm, Sun., 3 May

- 1. Is there any relation between the minimal polynomial and the characteristic polynomial?
- 2. What, if anything, does result 8.49 say about the multiplicity of each root of the minimal polynomial?
- 3. Show the details of the "simple computation" at the end of Example 8.50 that $(T-6I)(T-7I) \neq 0$.
- 4. Show the details of the "simple computation" at the end of Example 8.51 that (T-6I)(T-7I) = 0.
- B: Warmup exercises. For you to present in class. Due by the end of class Mon., 4 May Exercises 8.C: 1, 5.

Jordan Form

Section 8.D

A: Reading questions. Due by 2pm, Tue., 5 May

- 1. In Example 8.53, explicitly find the vectors N^3v , N^2v , and Nv. Use these to explicitly verify that the matrix of N with respect to the basis N^3v , N^2v , Nv, v is the one given in the example.
- 2. In Example 8.54, explicitly find the vectors N^2v_1, Nv_2 . Use these to explicitly verify that the matrix of N with respect to the basis $N^2v_1, Nv_1, v_1, N^2v, Nv_2, v_2, v_3$ is the one given in the example.
- 3. The linear operator T described in Examples 8.25 and 8.30 earlier in the chapter is *almost* put into Jordan Form in Example 8.30. Explain why this is *not* Jordan Form, and find the basis that will put it into Jordan Form. I think you should be able to do this only by following the proof of result 8.60 (Jordan Form) and the *statement* of result 8.55.
- 4. What will you do with all the time you have, now that there are no more reading questions to answer?
- B: Warmup exercises. For you to present in class. Due by end of class Wed., 6 May Exercises 8.D: 1, 2.