Math 4326/5322 Dr. Duval

## LINEAR ALGEBRA Homework

Wednesday, January 23

Follow the separate general guidelines for Parts A,B,C. Be sure to include and label *all* four standard parts (a), (b), (c), (d) of Part A in what you hand in.

## $\mathbf{R}^n$ and $\mathbf{C}^n$

## Section 1.A

A: Reading questions. Due by 2pm, Sun., 27 Jan.

- 1. Verify, using properties of real numbers, and that  $(-i)^2 = -1$ , that complex numbers satisfy the distributive property.
- 2. What does **F** stand for?
- 3. What two things does 0 stand for? Why do we use this same symbol for both of these things?
- 4. The picture for addition in  $\mathbf{F}^n$  on p. 9 is 2-dimensional (n = 2), since it is drawn on a 2-dimensional piece of paper. Does this picture work for larger values of n? Why or why not?
- 5. What gets multiplied in scalar multiplication?
- B: Warmup exercises. For you to present in class. Due by the end of class Mon., 28 Jan.Exercises 1.A: 2, 10, 15

## Definition of Vector Space Section 1.B

A: Reading questions. Due by 2pm, Tue., 29 Jan.

- 1. Verify commutativity in  $\mathbf{F}^{\infty}$ .
- 2. Verify distributivity in  $\mathbf{F}^{S}$ .
- 3. In the proof of result 1.26 (Unique additive inverse), why do we "[s]uppose that w and w' are additive inverses of v"?
- 4. In result 1.30 (A number times the vector 0), identify which properties of vector spaces are used at each step of the proof.
- 5. Result 1.31 (The number -1 times a vector) may seem unnecessary to prove. But (-1)v and -v are **defined** differently, if you look carefully at the definitions. How is each one defined?
- B: Warmup exercises. For you to present in class. Due by end of class Wed., 30 Jan. Exercises 1.B: 1, 3, 4