

Homework

Thursday, October 6

**Written homework.** None this week. (Study for the exam instead.)

**Warmup exercises.** To present in class.

**Tuesday, October 11.** 4.34, 4.37.

**Reading assignment.** These reading questions cover the rest of Section 4.3 (subsections on Units and Fields and on Subrings and Subfields).

1. Illustrate Proposition 4.39 when  $m = 5$  and  $m = 6$ . In each case, identify which elements of  $\mathbb{Z}_m$  have an inverse. For the ones that do have an inverse, find the inverse. (These examples are small enough that even guess and check is not a bad strategy).
2. The ring of  $2 \times 2$  matrices with real coefficients was described on p. 156. What are the units of this ring?
3. Answer the query at the top of p. 166: Is  $\mathbb{Z}_m$  a subring of  $Z$ ? Why or why not?
4. Consider Example 4.47 when  $X = \{p, q\}$ . Make the addition and multiplication tables for the ring  $2^X$ .