Math 5370 Dr. Duval

### GAME THEORY Homework

Wednesday, April 24

Follow the separate general guidelines for Parts A,B,C. Be sure to include and label *all* four standard parts (a), (b), (c), (d) of Part A in what you hand in.

### Two negative theorems; desirable properties

Sections 13.3, 13.4, 13.5

## A: Reading questions. Due by 3pm, Mon., 29 Apr.

- 1. Discuss Remark 13.3.2 and Figure 13.6. What is an argument that the relative ranking of A and B should be the same in both profiles of the figure? What is an argument that the relative ranking of A and B should be different in the different profiles of the figure.
- 2. Compare and contrast Arrow's Theorem and Gibbard-Satterthwaite Theorem. How are they similar and how are they different?
- 3. The examples in Figures 13.2 and 13.3 show how some voters can strategically change their votes to get a new outcome that they prefer to the original outcome. But it does **not** illustrate the Gibbard-Satterthwaite Theorem; explain why not.
- 4. Rank the five "desirable properties of voting systems beyond unanimity and IIA", from most important to least important, in your opinion. Explain your reasoning.
- B: Warmup exercises. For you to present in class. Due by the end of class Mon., 29 Apr.

Construct an example showing that plurality voting satisfies the Gibbard-Satterthwaite Theorem.

# Analysis of specific voting rules Section 13.6

### A: Reading questions. Due by 2pm, Tue., 30 Apr.

- 1. Apply each voting rule in this section to the examples in Figures 13.1, 13.2, and 13.3. For positional voting, have each voter assign 3 points to their top candidate, 1 point to their second-most-favorite candidate, and 0 points to their least favorite candidate. For approval voting, have each voter approve their top two preferences.
- B: Warmup exercises. For you to present in class. Due by end of class Wed., 1 May

Construct examples showing that each voting rule in this section satisfies the Gibbard-Satterthwaite Theorem.