Math 5370 Dr. Duval

#### GAME THEORY Homework

Wednesday, May 1

Follow the separate general guidelines for Parts A,B,C. Be sure to include and label *all* four standard parts (a), (b), (c), (d) of Part A in what you hand in.

## Proof of Arrow's Impossibility Theorem Section 13.7

#### A: Reading questions. Due by 2pm, Sun., 5 May

- 1. Give details how Figure 13.14 illustrates the proof of Lemma 13.7.1. In other words, match individual sentences in the proof to specific aspects of the diagram.
- 2. Draw a diagram illustrating the definition of *B*-**pivotal** voter. (Consider the other diagrams in this section as a model.) Give a little more detail about how the sentence following the definition ("Such a voter...") matches the precise definition given in Definition 13.7.2.
- 3. What earlier proof in Chapter 13 does the proof of Lemma 13.7.3 resemble?
- 4. Draw a more detailed version of Figure 13.16 with 5 voters, 6 candidates, and show not just  $\pi_3$ , but also  $\pi$ ,  $\pi_1$ , and  $\pi_2$ . Purposely pick  $\pi$  [say that three times fast] to best illustrate the proof of Lemma 13.7.4.
- B: Warmup exercises. For you to present in class. Due by the end of class Mon., 6 May None, but be ready to discuss the proof (given at the end of this section) of Theorem 13.3.1.

## **Proof of the Gibbard-Satterthwaite Theorem** Section 13.8

## A: Reading questions. Due by 2pm, Tue., 7 May

- 1. Where was the idea of Definition 13.8.1 used previously in this chapter (possibly in more than one place)?
- 2. Add to the Figure 13.17 by showing  $\pi_i$ . Now draw another version of  $\pi_i$  so that your two versions correspond to the "two cases to rule" at the top of p. 218.
- 3. Draw diagrams illustrating each of Definition 13.8.3 and Claim 13.8.4. (Consider the other diagrams in this section as a model.) Purposely pick  $\pi$  and S to best illustrate the definition and the claim. You may use different  $\pi$  and S for each of the two diagrams.

# B: Warmup exercises. For you to present in class. Due by end of class Wed., 8 May

None, but be ready to discuss the proof (given at the end of this section) of Theorem 13.4.2.