

Undesirable Habits of Mind of Pre-service Teachers

Kien Lim

University of Texas at El Paso

PME-NA Conference

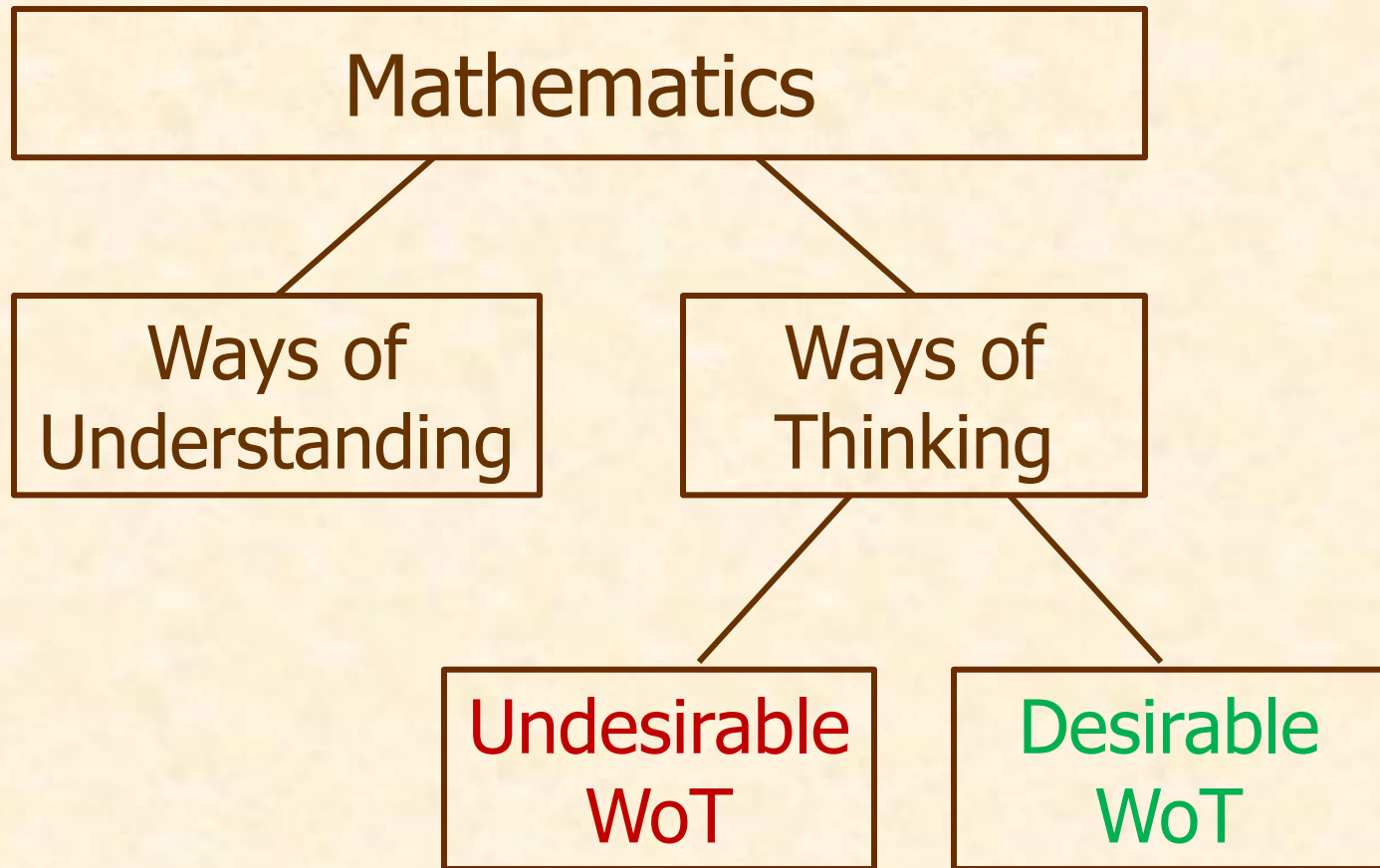
Sep 24, 2009

Atlanta, GA

Outline of Presentation

- Undesirable Ways of Thinking
- Impulsive Disposition
- Pedagogical Suggestions for Addressing Impulsive Disposition
- Some Encouraging Results
- Students' Written Comments

Undesirable Ways of Thinking



Undesirable Ways of Thinking

1. Beliefs

- **Mathematics** is a collection of rules and procedures.
- “**Doing mathematics** means following the rules laid down by the teacher, **knowing mathematics** means remembering and applying the correct rule when the teacher asks a question, and **mathematical truth** is determined when the answer is ratified by the teacher.”

(Lampert, 1990, p. 31)

Undesirable Ways of Thinking

1. Beliefs

- Mathematics is a collection of rules and procedures.

2. Proof-schemes

- Authoritative proof scheme
- Empirical proof scheme (Harel & Sowder, 1998)

3. Problem-solving approaches

- “Waiting to be told what to do”
- “Doing whatever first comes to mind ... or diving into the first approach that comes to mind”

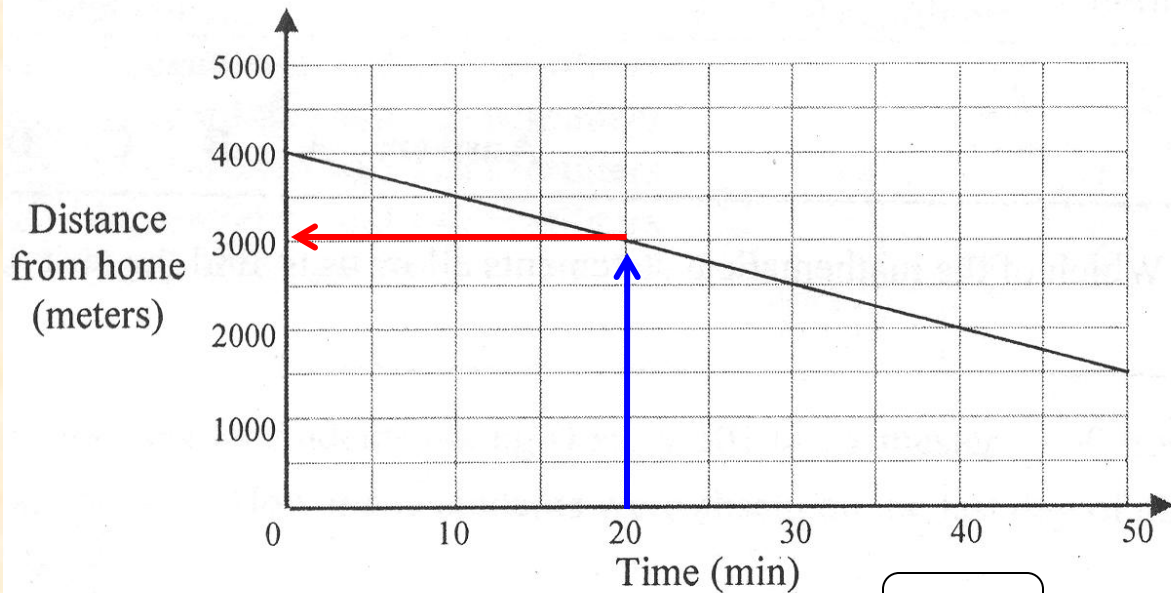
Impulsive
Disposition

(Watson & Mason, 2007, p. 207)

Impulsive Disposition

An Example

Gina is traveling home from her friend's house. The graph represents a portion of Gina's journey. What is Gina's speed at the 20th minute?



$$\begin{aligned} \text{Speed} &= \frac{d}{t} \\ &= \frac{3000}{20} \\ &= 150 \end{aligned}$$

$$\begin{array}{r} 150 \\ 20 \overline{) 3000} \\ \underline{20} \\ 100 \end{array}$$

- (a) Approximately 3000 meters
- (b) Approximately 50 meters/min
- (c) Approximately 80 meters/min
- (d) Approximately 150 meters/min

28%

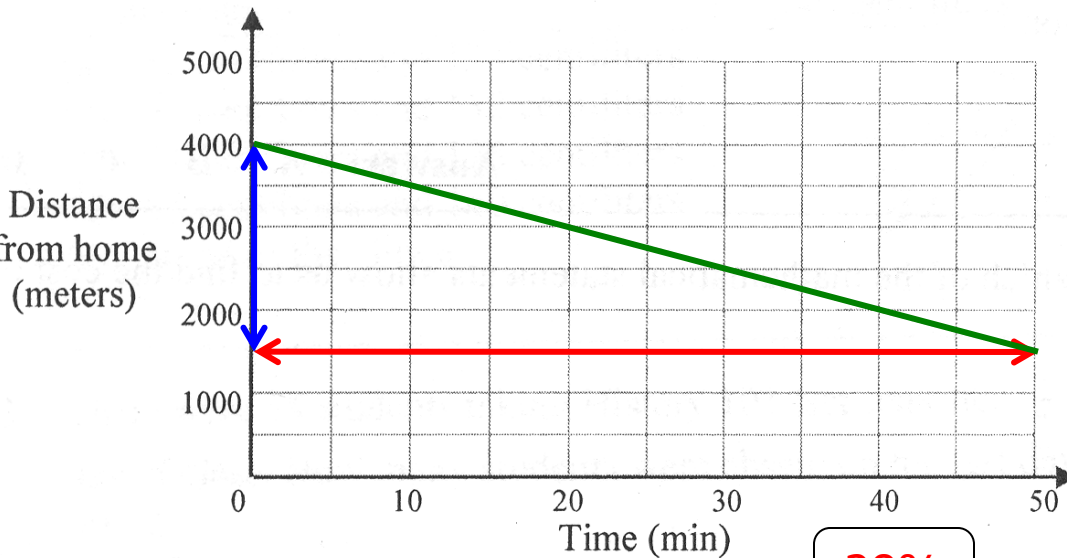
52%

Answer: A B C **D**

Impulsive Disposition

An Example

Gina is traveling home from her friend's house. The graph represents a portion of Gina's journey. What is Gina's speed at the 20th minute?



$$\frac{4000 - 1500}{50} = 50$$

- (a) Approximately 3000 meters 28%
- (b) Approximately 50 meters/min 18%
- (c) Approximately 80 meters/min
- (d) Approximately 150 meters/min 52%

Answer: A B C D

Impulsive Disposition

Two Possible Explanations

- Human Nature

“Our thinking is canalized with respect to the way we have learned to deal with things ... we implicitly anticipate that similar issues have similar causes, and thus similar solutions.” (Reigler, 2001, p. 535)

- School Effect (i.e. Nurture)

- Compartmentalization of school mathematics
- Emphasis on procedures for solving routine problems

Pedagogical Suggestions

- Do not teach algorithms/formulas prematurely
- Pose problems that
 - necessitate a particular algorithm/concept

A new housing subdivision offers rectangular lots of three different sizes:

- a. 75 feet by 114 feet
- b. 455 feet by 508 feet
- c. 185 feet by 245 feet

If you were to view these lots from above, which would appear most square?

(Simon & Blume, 1994)

Pedagogical Suggestions

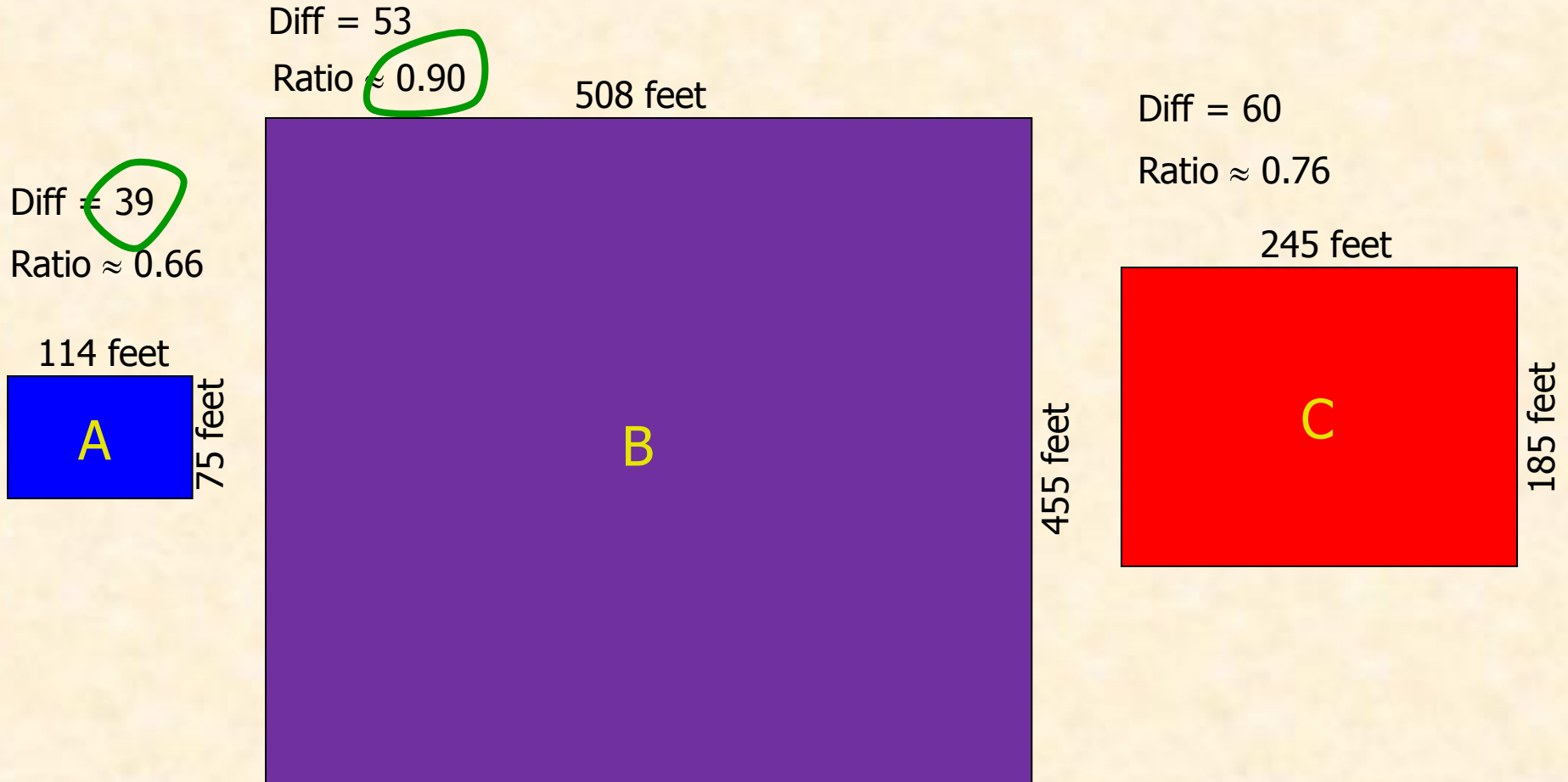
- Do not teach algorithms/formulas prematurely
- Pose problems that
 - necessitate a particular algorithm/concept

“Students are most likely to learn when they see a need for what we intend to teach them, where by ‘need’ is meant intellectual need, not social or economic need.” (Harel, 1998, p. 501)

Pedagogical Suggestions

- Do not teach algorithms/formulas prematurely
- Pose problems that
 - necessitate a particular algorithm/concept
 - intrigue students

Intriguing Students

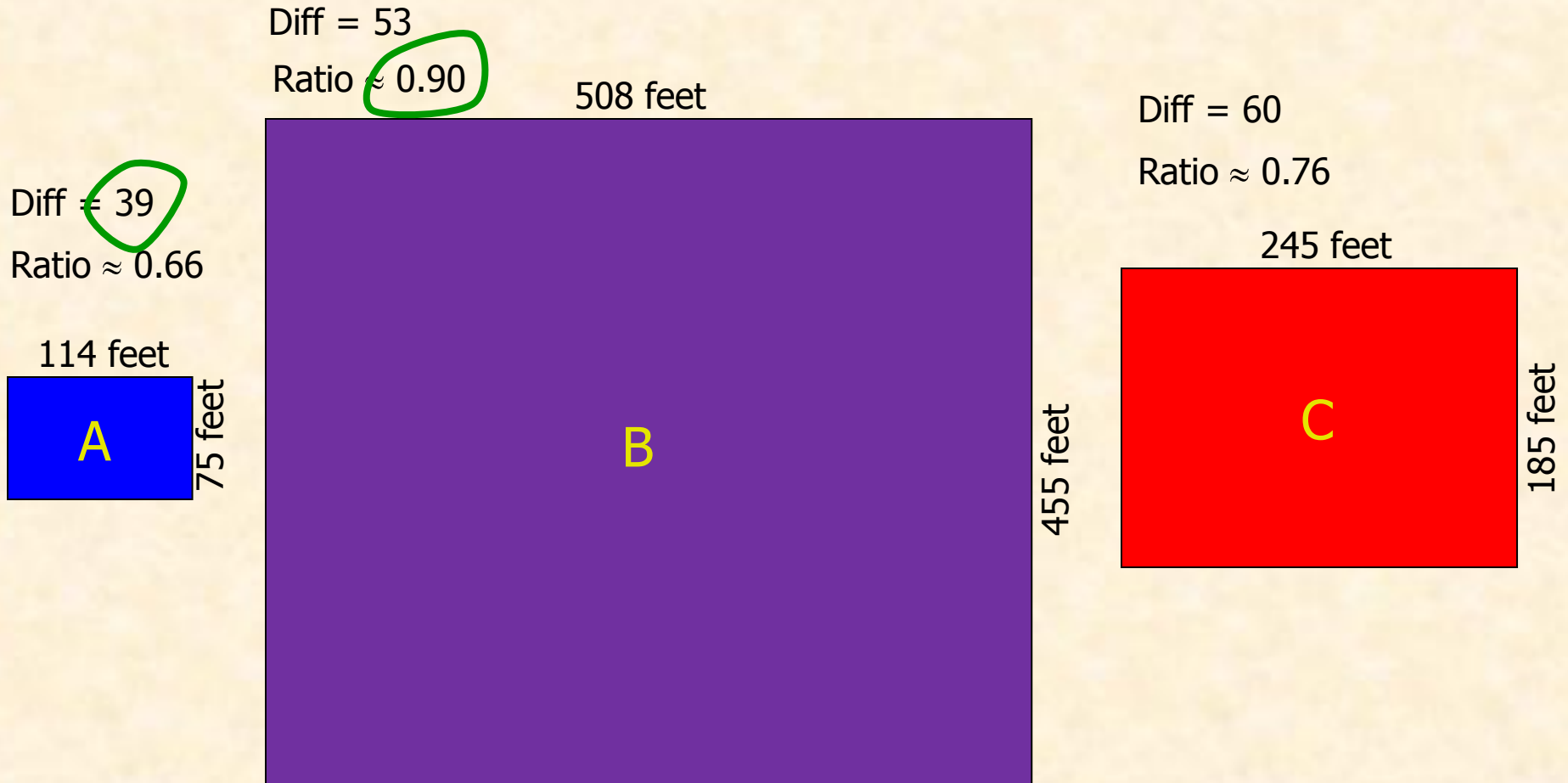


Question: Which method should I use?

Pedagogical Suggestions

- Do not teach algorithms/formulas prematurely
- Pose problems that
 - necessitate a particular algorithm/concept
 - intrigue students
 - require students to attend to meaning of numbers/symbols

Attending to Meaning



Question: What does 39 mean? What does 0.90 mean?

Attending to Meaning

Diff = 53

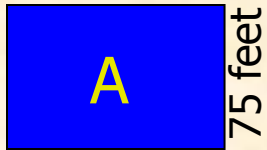
Ratio ≈ 0.90

508 feet

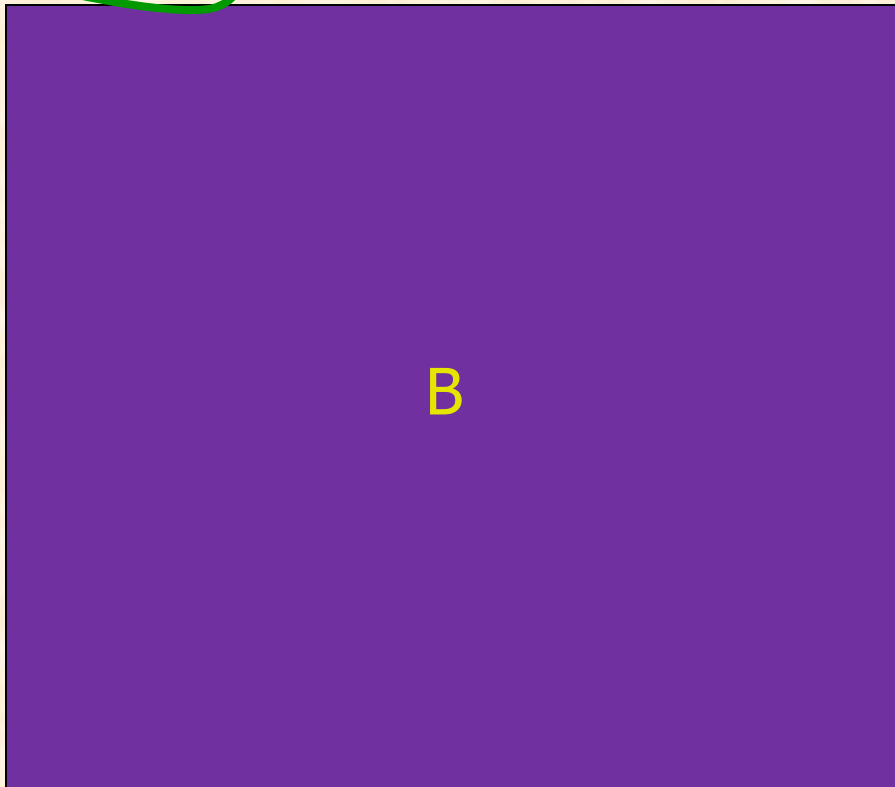
Diff = 39

Ratio ≈ 0.66

114 feet



75 feet

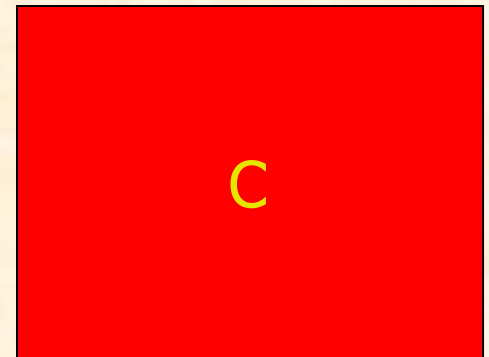


Diff = 60

Ratio ≈ 0.76

245 feet

455 feet



185 feet

$$\text{Ratio} = \frac{\text{Width}}{\text{Length}}$$

Ratio as a multiplicative comparison

455 feet is 0.9 times of 508 feet

Question: What does 0.90 mean?

Pedagogical Suggestions

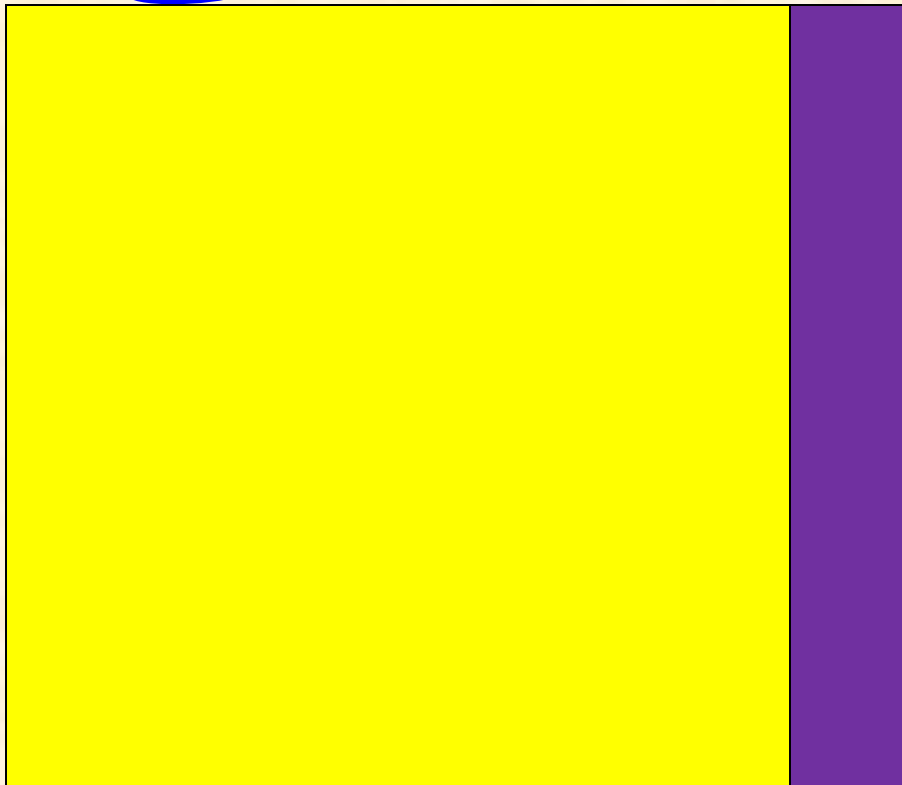
- Do not teach algorithms/formulas prematurely
- Pose problems that
 - necessitate a particular algorithm/concept
 - intrigue students
 - require students to attend to meaning of numbers/symbols
 - require students to explain and justify

Explaining & Justifying

Diff = 53

Ratio ≈ 0.90

508 feet

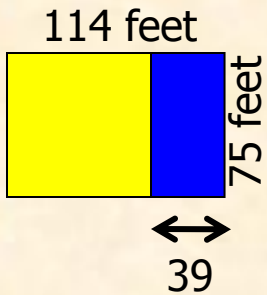


455 feet

53

Diff = 39

Ratio ≈ 0.66



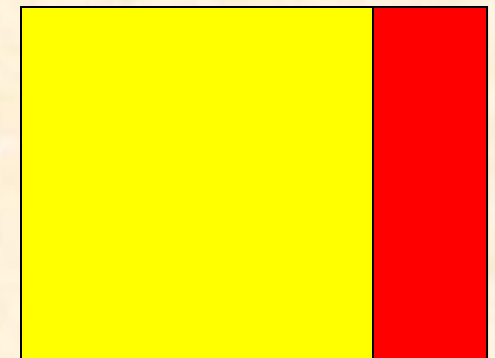
$$114 - 75 = 39$$

$$40 - 1 = 39$$

Diff = 60

Ratio ≈ 0.76

245 feet



185 feet

60

Difference = Length - Width

$$\text{Ratio} = \frac{\text{Width}}{\text{Length}}$$

$$= \frac{\text{Width} \times \text{Width}}{\text{Length} \times \text{Width}}$$

$$= \frac{\text{Area of Square}}{\text{Area of Rectangle}}$$

Question: Why is the ratio method better than the difference method?

Pedagogical Suggestions

- Do not teach algorithms/formulas prematurely
- Pose problems that
 - necessitate a particular algorithm/concept
 - intrigue students
 - require students to attend to meaning of numbers/symbols
 - require students to explain and justify
- Include contra-problems to promote skepticism

Promoting Sense-making

Sharon and Terri were comparing the size of their palms. Who do you think has a larger palm?

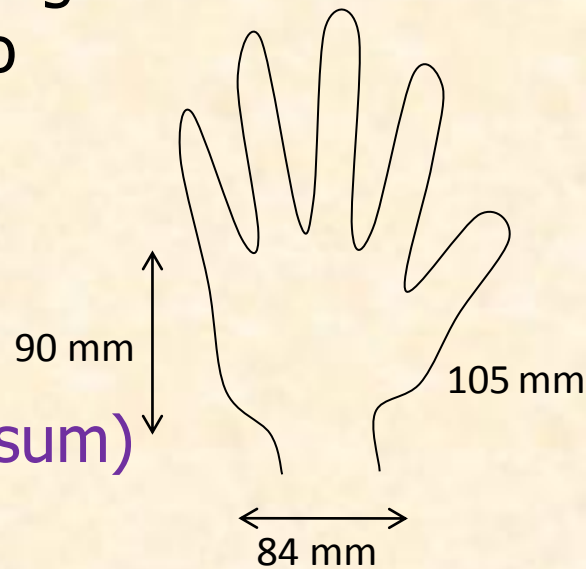
21% compared ratios

16% compared differences

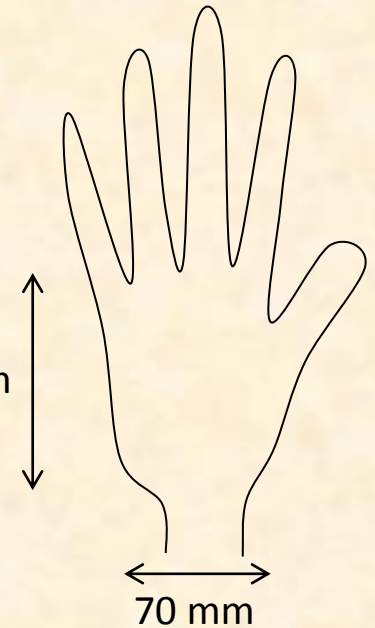
13% others (e.g. perimeters, sum)

49% compared areas

Sharon's hand



Terri's hand



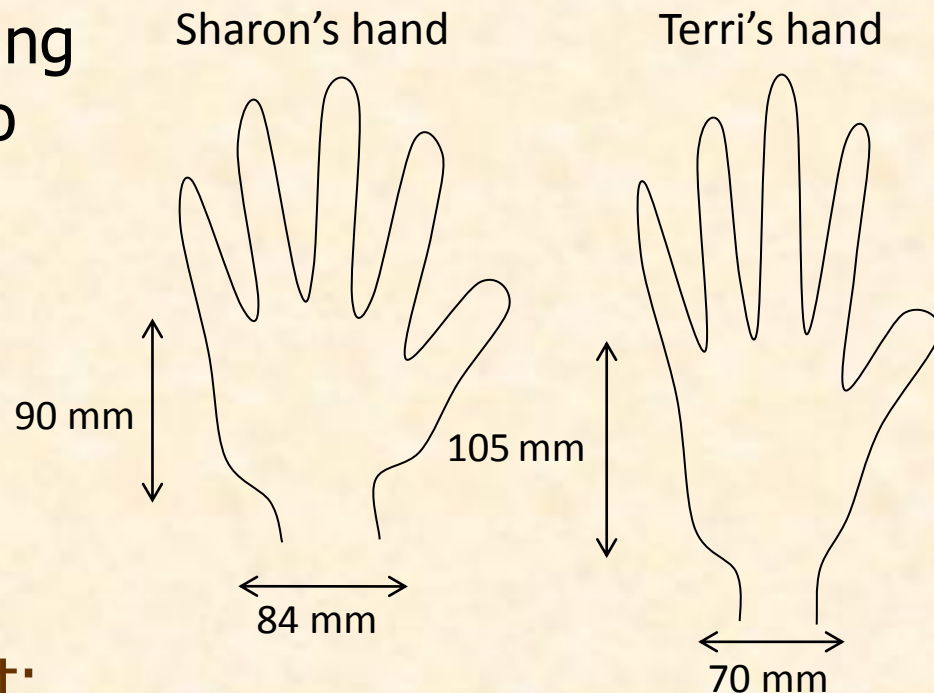
$$\frac{90}{84} = 1.071 \quad \frac{105}{70} = 1.5$$

Terri has a bigger palm because the ratio of her palm's height to her width is greater than Sharon's.

Fall 08
(61 students)

Promoting Sense-making

Sharon and Terri were comparing the size of their palms. Who do you think has a larger palm?



A Student's Written Comment:

"Dr. Lim had the great art of using awesome little tricks that would make us think [that] you [should] use ratios, for example, when in fact it was multiplication! This was a great tactic, because **often I would rush right into what I had just been taught**, not even looking into the problem."

Pedagogical Suggestions

- Do not teach algorithms/formulas prematurely
- Pose problems that
 - necessitate a particular algorithm/concept
 - intrigue students
 - require students to attend to meaning of numbers/symbols
 - require students to explain and justify
- Include contra-problems to promote skepticism
- Include superficially-similar-but-structurally-equivalent problems in tests and exams

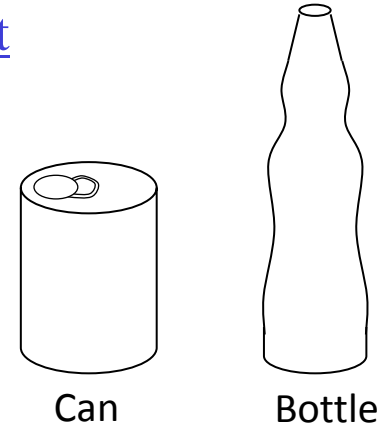
Some Encouraging Results

Direct-Proportional Item [Fall 07 \(47 students\)](#) [Fall 08 \(66 students\)](#)

The ratio of the amount of soda in the can to the amount of soda in the bottle is 4:3. There are 12 fluid ounces of soda in the can, how many fluid ounces of soda are in the bottle? [Pretest](#) [Posttest](#) [Pretest](#) [Posttest](#)

- (a) 8 fluid ounces
- (b) 9 fluid ounces
- (c) 15 fluid ounces
- (d) 16 fluid ounces
- (e) None of the above


55%  79% 63%  77%



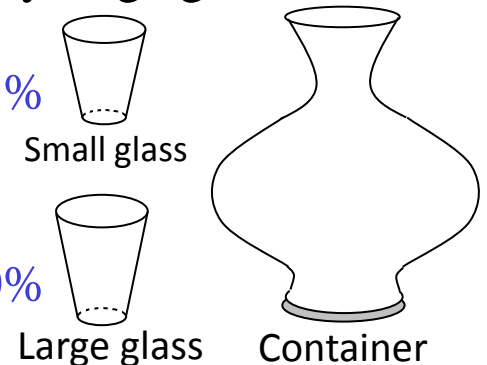
Inverse-Proportional Item

The ratio of the volume of a small glass to the volume of a large glass is 3:5. If it takes 15 small glasses to fill the container, how many large glasses does it take to fill the container?

- (a) 9 glasses
- (b) 13 glasses
- (c) 17 glasses
- (d) 25 glasses
- (e) None of the above

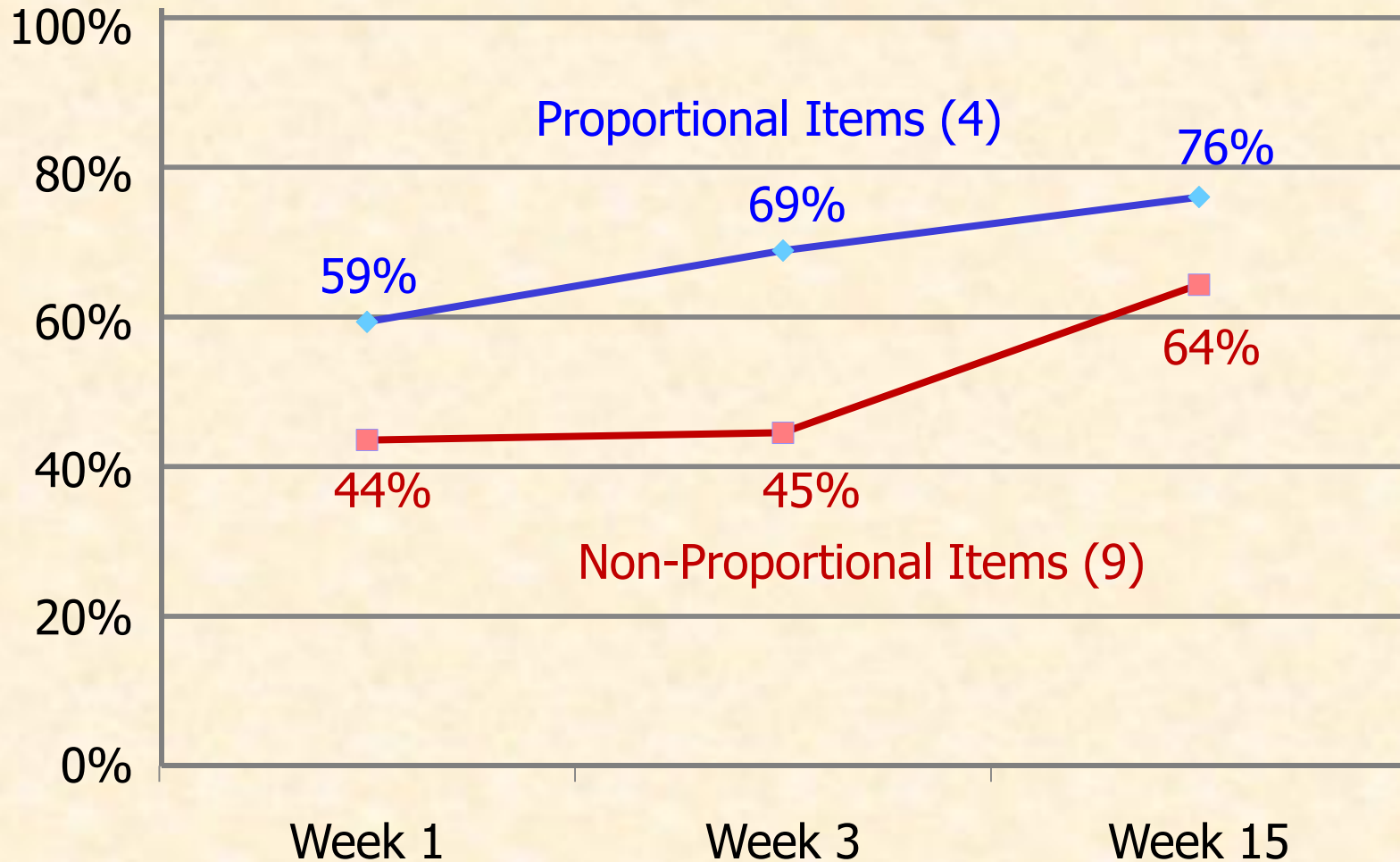
62%  43% 34%  73%

28%  45% 40%  20%



Some Encouraging Results

Fall 08 (66 students)



ASSESSING PROBLEM-SOLVING DISPOSITIONS: LIKELIHOOD-TO-ACT SURVEY

**Kien Lim, Osvaldo Morera, & Mourat Tchoshanov
University of Texas at El Paso**

**Sep 25, 2009 (8:20am – 9:00am)
Chestnut Room**

Students' Written Comments

- Do not teach algorithms/formulas prematurely

“My experience in this course was different from that in other classes because in this class ... explanation did not come until after we worked on the problem, or after we were assessed. ... It has been difficult for me to do math this new way, because I have been taught a different way of doing math for over twelve years. It would take more than just one semester of this kind of math for me to actually make it a habit.

- Include problems that require thinking in quizzes, tests and exams

Students' Written Comments

"I learned to **analyze the problem** instead of **rushing into a procedure**, I used to do that."

- Pose problems that
 - necessitate a particular algorithm/concept
 - intrigue students
 - require students to attend to meaning of numbers/symbols
 - require students to explain and justify

"I think that this class helped me ... by **thinking deeper about that problem** instead of **just looking at the numbers and wanting to do something with them.**"

tests and exams

S,

Students' Written Comments

- Do not teach algorithms/formulas prematurely
- Pose problems that
 - necessitate a particular algorithm/concept

"In this class, the concepts remain the same, yet the **problems themselves are always quite different**. I can no longer **rely on 'similar problems'** in order to figure out my homework or pass [the] exams."

- Include contra-problems to promote skepticism
- Include problems that require thinking in quizzes, tests and exams

Students' Written Comments

"This class is very demanding because I have to dedicate more time to learn how to get rid of those "bad habits" that I have learned in previous classes."

"It would take more than just one semester of this kind of math for me to actually make it a habit."

Thank You