# Michigan Math. J. 0 (2016), 1–11

1		1
2		2
3	Twisting of Composite Torus Knots	3
4		4
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6	APSTRACT. We prove that the family of connected sums of torus knots	6
7	T(2, p) # T(2, q) # T(2, r) is nontwisted for any odd positive integers	7
8	p, q, r > 3, partially answering in the positive a conjecture of Tera-	8
9	gaito [22].	9
10		10
10		12
13	1. Introduction	13
14	Let K be a knot in the 3-sphere $S^3$ and $D^2$ a disk intersecting K in its interior	14
15	Let <i>n</i> be an integer A $(-\frac{1}{2})$ -Dehn surgery along $C = \partial D^2$ changes K into a new	15
16	knot K in $S^3$ Let $\omega = lk(\partial D^2 I)$ We say that K is obtained from K by $(n, \omega)$ -	16
17	where $K_{\eta}$ in $S$ . Let $\omega = i K(\delta D^{-}, D)$ , we say that $K_{\eta}$ is obtained from $K$ by $(n, \omega)$	17
18	twisting (or simply twisting). Then we write $K \to K_n$ or $K \to K(n, \omega)$ . We	18
19	say that $K_n$ is an $(n, \omega)$ -twisted knot (or simply a twisted knot) if K is the unknot	19
20	(See Figure 1).	20
21	An easy example is depicted in Figure 2, where we show that the right-handed trefoil $T(2, 3)$ is obtained from the unknot $T(2, 1)$ by a $(\pm 1, 2)$ twisting (in this	21
22	case $n = \pm 1$ and $\omega = \pm 2$ ) A less obvious example is given in Figure 3 where	22
23	it is shown that the composite knot $T(2, 3) \# T(2, 5)$ can be obtained from the	23
24	unknot by a (+1, 4)-twisting (in this case, $n = +1$ and $\omega = +4$ ); see [13]. Here,	24
25	T(2, q) denotes the $(2, q)$ -torus knot (see [14]).	25
26	Active research on twisting of knots started around 1990. One pioneer was	26
27	the author's Ph.D. thesis advisor Y. Mathieu, who asked the following questions	27
28	in [16].	28
29	2	29
31	QUESTION 1.1. Is every knot in S <sup>5</sup> twisted? If not, what is the minimal number	31
32	of twisting disks?	32
33	OUESTION 1.2 Is every twisted knot in $S^3$ prime?	33
34	QUESTION 1.2. IS every twisted kilot in 5° prime.	34
35	To answer Question 1.1, Miyazaki and Yasuhara [18] were the first to give an	35
36	infinite family of knots that are nontwisted. In particular, they showed that the	36
37	granny knot, that is, the product of two right-handed trefoil knots, is the smallest	37
38	nontwisted knot. In his Ph.D. thesis [3], the author showed that $T(5, 8)$ is the	38
39	smallest nontwisted torus knot. This was followed by a joint work with Yasuhara	39
40	[5], in which we gave an infinite family of nontwisted torus knots (i.e., $T(p, p+7)$	40
41	for any $p \ge 7$ ) using some techniques derived from old gauge theory. On the other	41
42	hand, Ohyama [19] showed that any knot in $S^3$ can be untied by (at most) two	42
43	disks.	43
44	Paceived July 12, 2015 Pavision received March 0, 2016	44
45	Received July 12, 2013. Revision received initial 9, 2010.	45
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independently found examples of composite twisted knots (see Figure 3). In particular, Goodman-Strauss [11] showed that any composite knot of the form T(p,q) # T(-q, p+q) is a twisted knot for any coprime positive integers 1 . More generally, Hayashi and Motegi [13] and Goodman-Strauss [11]proved independently that only single twisting (i.e., |n| = 1) can yield a compos-ite knot. The tools used were combinatorial methods as in CGLS [8]. Moreover, Goodman-Strauss [11] proved that  $K_1$  and  $K_{-1}$  cannot both be composite and classified all composite knots of the form  $K_1 \# K_2$ , where  $K_1$  and  $K_2$  are both prime knots (for an extensive list of twisted composite knots, we refer the reader to the appendix of Goodman-Strauss's paper [11]). However, there is no known twisted knot with three or more factors, that is,  $k = k_1 \# k_2 \# \cdots \# k_m$ , where  $k_i$ 

is a prime knot for i = 1, 2, ..., m, and  $m \ge 3$ , which motivates the still open Teragaito's conjecture. CONJECTURE 1.1 (Teragaito [22]). Any composite knot with three or more factors is nontwisted. In this paper, we prove the following theorem. THEOREM 1.1. T(2, p) # T(2, q) # T(2, r) is not twisted for any odd positive in-tegers  $p, q, r \geq 3$ . 2. Preliminaries In what follows, let X be a smooth, closed, oriented, simply connected 4-manifold. Then the second homology group  $H_2(X; \mathbb{Z})$  is finitely generated (for details, we refer to the book by Milnor and Stasheff [17]). The ordinary form  $q_X: H_2(X; \mathbb{Z}) \times H_2(X; \mathbb{Z}) \longrightarrow \mathbb{Z}$  given by the intersection pairing for 2-cycles such that  $q_X(\alpha, \beta) = \alpha \cdot \beta$  is a symmetric unimodular bilinear form. The sig-nature of this form, denoted  $\sigma(X)$ , is the difference of the numbers of pos-itive and negative eigenvalues of a matrix representing  $q_X$ . Let  $b_2^+(X)$  (resp.  $b_2^{-}(X)$ ) be the rank of the positive (resp. negative) part of the intersection form of X. The second Betti number is  $b_2(X) = b_2^+(X) + b_2^-(X)$ , and the signature is  $\sigma(X) = b_2^+(X) - b_2^-(X)$ . From now on, a homology class in  $H_2(X - B^4, \partial; \mathbb{Z})$ is identified with its image by the homomorphism  $H_2(X - B^4, \partial(X - B^4); \mathbb{Z}) \cong H_2(X - B^4; \mathbb{Z}) \longrightarrow H_2(X; \mathbb{Z}).$ Recall that  $\mathbb{CP}^2$  is the closed 4-manifold obtained by the free action of  $\mathbb{C}^* = \mathbb{C} - \{0\}$  on  $\mathbb{C}^3 - \{(0, 0, 0)\}$  defined by  $\lambda(x, y, z) = (\lambda x, \lambda y, \lambda z)$ , where  $\lambda \in \mathbb{C}^*$ , that is,  $\mathbb{CP}^2 = (\mathbb{C}^3 - \{(0, 0, 0)\})/\mathbb{C}^*$ . An element of  $\mathbb{CP}^2$  is denoted by its homogeneous coordinates [x : y : z], which are defined up to the multipli-cation by  $\lambda \in \mathbb{C}^*$ . The fundamental class of the submanifold  $H = \{[x : y : z] \in$  $\mathbb{CP}^2|x=0\}$   $(H \cong \mathbb{CP}^1)$  generates the second homology group  $H_2(\mathbb{CP}^2;\mathbb{Z})$  (see Gompf and Stipsicz [11]). Since  $H \cong \mathbb{CP}^1$ , the standard generator of  $H_2(\mathbb{CP}^2; \mathbb{Z})$ is denoted, from now on, by  $\gamma = [\mathbb{CP}^1]$ . Therefore, the standard generator of  $H_2(\mathbb{CP}^1, \mathbb{Z})$   $H_2(\mathbb{CP}^2 - B^4; \mathbb{Z})$  is  $\mathbb{CP}^1 - B^2 \subset \mathbb{CP}^2 - B^4$  with complex orientations. Let  $\alpha = S^2 \times \{\star\}$  and  $\beta = \{\star\} \times S^2$  denote the standard generators of  $H_2(S^2 \times S^2; \mathbb{Z})$  such that  $\alpha^2 = \beta^2 = 0$ ,  $\alpha \cdot \beta = 1$ , and let  $\gamma$  (resp.  $\overline{\gamma}$ ) be the standard generators of  $H_2(\mathbb{CP}^2; \mathbb{Z})$  (resp.  $H_2(\mathbb{CP}^2; \mathbb{Z})$ ) with  $\gamma^2 = +1$  (resp.  $\bar{\gamma}^2 = -1$ ). A second homology class  $\xi \in H_2(X; \mathbb{Z})$  is said to be characteristic if  $\xi$  is dual to the second Stiefel–Whitney class  $w_2(X)$  or, equivalently,  $\xi \cdot x \equiv x \cdot x \pmod{2}$ for any  $x \in H_2(X; \mathbb{Z})$  (we leave the details to Milnor and Stasheff [17]). 

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1 2 3 4 5 6 7 8 9 10 11	EXAMPLE 2.1. $(a, b) \in H_2(S^2 \times S^2; \mathbb{Z})$ is characteristic if and only if <i>a</i> and <i>b</i> are both even.	1 2 2		
	EXAMPLE 2.2. $d\gamma \in H_2(\mathbb{CP}^2; \mathbb{Z})$ is characteristic if and only if <i>d</i> is odd.	4		
	The following theorems give obstructions on the genus of an embedded surface representing either a characteristic class or bounding a knot in a punctured 4-manifold. Recall that the Arf invariant of a knot <i>K</i> is denoted by $\operatorname{Arf}(K)$ , $\sigma_p(K)$ denotes the Tristram <i>p</i> -signature [24], and $e_2(K)$ denotes the minimum number of generators of $H_2(X_K; \mathbb{Z})$ , where $X_K$ is the 2-fold branched covering of $S^3$ along <i>K</i> .			
12 13 14	THEOREM 2.1 (Acosta [1]). Suppose that $\xi$ is a characteristic homology class in an indefinite smooth oriented 4-manifold of genus g. Let $m = \min(b_2^+(X), b_2^-(X))$ .	12 13 14		
16 17 18	(1) If $\xi^2 \equiv \sigma(X) \mod 16$ , then either $\xi^2 = \sigma(X)$ or, if not, (a) If $\xi^2 = 0$ or $\xi^2$ and $\sigma(X)$ have the same sign, then $ \xi^2 - \sigma(X) /8 \le m + g - 1$ . (b) If $\sigma(X) = 0$ or $\xi^2$ and $\sigma(X)$ have opposite signs, then $ \xi^2 - \sigma(X) /8 \le m + g - 1$ .	16 17 18		
19 20 21 22	<ul> <li>(b) If σ(X) = 0 or ξ<sup>2</sup> and σ(X) have opposite signs, then  ξ<sup>2</sup> = σ(X) /8 ≤ m + g - 2.</li> <li>(c) If ξ<sup>2</sup> ≡ σ(X) + 8 mod 16, then</li> <li>(a) If ξ<sup>2</sup> = -8 or ξ<sup>2</sup> + 8 and σ(X) have the same sign, then  ξ<sup>2</sup> + 8 - σ(X) /8 ≤ m + g + 1.</li> </ul>	19 20 21 22		
23 24 25 26	(b) If $\sigma(X) = 0$ or $\xi^2 + 8$ and $\sigma(X)$ have opposite signs, then $ \xi^2 + 8 - \sigma(X) /8 \le m + g$ .	23 24 25		
20 27 28 29	THEOREM 2.2 (Gilmer [10] and Viro [25]). Let X be an oriented compact 4- manifold with $\partial X = S^3$ , and K a knot in $\partial X$ . Suppose that K bounds a surface of genus g in X representing an element $\xi$ in $H_2(X; \partial X)$ .	20 27 28 29		
30 31 32	<ol> <li>(1) If ξ is divisible by an odd prime d, then  (d<sup>2</sup> − 1)/(2d<sup>2</sup>)ξ<sup>2</sup> − σ(X) − σ<sub>d</sub>(K)  ≤ dim H<sub>2</sub>(X; Z<sub>d</sub>) + 2g.</li> <li>(2) If ξ is divisible by 2, then  ξ<sup>2</sup>/2 − σ(X) − σ(K)  ≤ dim H<sub>2</sub>(X; Z<sub>2</sub>) + 2g.</li> </ol>	30 31 32		
33 34 35 36	THEOREM 2.3 (Robertello [20]). Let X be an oriented compact 4-manifold with $\partial X = S^3$ , and K a knot in $\partial X$ . Suppose that K bounds a disk in X representing a characteristic element $\xi$ in $H_2(X; \partial X)$ . Then $(\xi^2 - \sigma(X))/8 \equiv \operatorname{Arf}(K) \pmod{2}$ .	33 34 35 36		
37 38 39 40	LEMMA 2.1. If <i>K</i> is a knot obtained by a $(-1, \omega)$ -twisting from the unknot $K_0$ , then <i>K</i> bounds a properly embedded smooth disk $(D, \partial D) \subset (\mathbb{CP}^2 - B^4, \partial(\mathbb{CP}^2 - B^4))$ such that $[D] = \omega \gamma \in H_2(\mathbb{CP}^2 - B^4, \partial(\mathbb{CP}^2 - B^4); \mathbb{Z})$ .	37 38 39 40		
41 42 43 44 45 46	Recall, for convenience of the reader, a proof of Lemma 2.1. As shown in Figure 4, let <i>D</i> be a disk on which the $(-1, \omega)$ -twisting is performed. Note that the $(+1)$ -Dehn surgery on $\partial D = C$ changes $K_0$ to <i>K</i> . Regard $K_0$ and <i>D</i> as contained in the boundary of a four-dimensional 0-handle $h^0$ . Then attach a 2-handle $h^2$ to $h^0$ along $\partial D$ with framing +1. Since $\mathbb{CP}^2 = h^0 \cup h^2 \cup h^3$ with $h^0 \cong B^4$ and $h^3 \cong$	41 42 43 44 45 46		





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$$[D] = \omega\gamma \in H_2(\mathbb{CP}^2 - B^4, S^4; \mathbb{Z})$$

$$[D] = \omega\gamma \in H_2(\mathbb{CP}^2 - B^4, S^4; \mathbb{Z})$$

$$[\Delta] = 2u + (g^t + l)\beta \in H_2(S^2 \times S^2 - B^4, S^3; \mathbb{Z})$$

$$Figure 9$$
The genus-two smooth and closed surface  $\Sigma = F \cup D$  satisfies
$$[\Sigma] = 2\alpha + (g^s + \ell)\beta + \omega\gamma \in H_2(S^2 \times S^2 \# \mathbb{CP}^2; \mathbb{Z}).$$
By Lemma 2.2,  $\omega$  is odd, and by Proposition 3.1,  $g^s + \ell$  is even. Then,  $\xi = [\Sigma]$ 
is a characteristic class in  $H_2(S^2 \times S^2 \# \mathbb{CP}^2; \mathbb{Z}).$ 
By Lemma 2.2,  $\omega$  is odd, and by Proposition 3.1,  $g^s + \ell$  is even. Then,  $\xi = [\Sigma]$ 
is a characteristic class in  $H_2(S^2 \times S^2 \# \mathbb{CP}^2; \mathbb{Z}).$ 
Furthermore,  $X = S^2 \times S^2 \# \mathbb{CP}^2$ 
is homeomorphic to  $\mathbb{CP}^2 \# \mathbb{CP}^2 \oplus \mathbb{CP}^2$  (e.g., see Scorpan's book [21], p. 239, or Corollary 4.3 in Kirby's book [15], p. 11). Note that  $\xi^2$  and  $\sigma(X)$  have the same signs,  $m = 1$ , and  $g = 2$ . Therefore, by Theorem 2.1(1)(a) and Theorem 2.1(2)(a),  $\frac{|\xi^2 - \sigma(X)|}{8} \leq 3$ 
or, equivalently,
 $\frac{4(g^s + \ell) + \omega^2 - 1}{8} \leq 3.$ 
This yields that the only possibilities are  $g^s = 3$  or 4 and  $\omega = \pm 1$ ; equivalently,  $K = T(2, 3) \# T(2, 3) \# T(2, 3)$ , then  $\ell = 3$  or  $K = T(2, 3) \# T(2, 3) \# T(2, 3)$ , then  $\ell = 3$  or  $K = T(2, 3) \# T(2, 3) \# T(2, 3)$ , then  $\ell = 2$  with  $\omega = \pm 1$ . Then K would bound a disk  $(D, \partial D) \subset (\overline{\mathbb{CP}^2} - B^4, \partial(\overline{\mathbb{CP}^2} - B^4); \mathbb{Z})$ ,
where  $\tilde{\gamma}$  is the standard generator of  $H_2(\overline{\mathbb{CP}^2} - B^4, \partial(\overline{\mathbb{CP}^2} - B^4); \mathbb{Z})$ , where  $\tilde{\gamma}$  is the standard generator of  $H_2(\overline{\mathbb{CP}^2} - B^4); \mathbb{Z})$ , with  $\tilde{\gamma}^2 = -1$ , and therefore  $|\xi^2 - \sigma(X)|/8 = 0$ . This contradicts Theorem 2.3 since  $Art(K) = 1$ .

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	1	Case II. Assume that $n = -1$ . Then there are two cases to exclude.	1
	2	Case II(a). If $\omega$ is divisible by a prime $d \ge 3$ , then by Lemma 2.1, k	2
	3	bounds a smooth disk $(D, \partial D) \subset (\mathbb{CP}^2 - B^4, \partial(\mathbb{CP}^2 - B^4) \cong S^3)$ such that	3
	4	$\xi = [D] = \omega \gamma \in H_2(\mathbb{CP}^2 - B^4; S^3; \mathbb{Z})$ . By Lemma 2.3 the signatures are	4
	5	$\sigma(K) = -(p+q+r-3) \text{ and }$	5
	6	$\begin{bmatrix} n \end{bmatrix} \begin{bmatrix} a \end{bmatrix} \begin{bmatrix} r \end{bmatrix}$	6
	7	$\sigma_d(K) = -(p-1) - \left  \frac{r}{2d} \right  - (q-1) - \left  \frac{4}{2d} \right  - (r-1) - \left  \frac{1}{2d} \right   (\text{see } [2]).$	7
	8	This contradicts Theorem 2.2	8
	9	This contradicts Theorem 2.2. Case II(b) If $\alpha = \pm 1$ then by the same argument as in Case I this would yield	9
	10	Case $\Pi(0)$ . If $\omega = \pm 1$ , then by the same argument as $\Pi$ case 1, this would yield the existence of a genus two surface that satisfies	10
	10		10
	12	$\xi = [\Sigma] = 2\alpha + (g^* + \ell)\beta + \bar{\gamma} \in H_2(S^2 \times S^2 \# \mathbb{CP}^2; \mathbb{Z}).$	12
	14	If we let $X = S^2 \times S^2 \# \overline{\mathbb{CP}^2}$ , then $\xi^2$ and $\sigma(X)$ have opposite signs with $m = 1$	14
	15	and $g = 2$ . Therefore, by Theorem 2.1(1)(b) and Theorem 2.1(2)(b).	15
	16	$ \mathcal{E}^2 - \mathcal{C}(\mathbf{V}) $	16
	17	$\frac{ \varsigma - \sigma(\Lambda) }{2} \le 2$	17
	18	8	18
	19	or, equivalently, $g^* + \ell \le 4$ . This yields that the only possibilities are $g^* = 3$ or	19
	20	4; equivalently, $K = T(2,3) \# T(2,3) \# T(2,3)$ , then $\ell = 3$ or $K = T(2,3) \#$	20
	21	$T(2,3) \# T(2,5)$ , and then $\ell = 2$ . Therefore, $g^* + \ell = 6$ , a contradiction.	21
	22	ACKNOWLEDGMENTS I would like to thank the referee for his valuable sug-	22
	23	gestions and the University of El Paso at Teyas (UTEP) Mathematical Sciences	23
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	24	Department for hospitality	24
	24 25	Department, for hospitality.	24 25
	24 25 26	Department, for hospitality. References	24 25 26
	24 25 26 27	References	24 25 26 27
	25 26 27 28	Department, for hospitality.         References         [1] D. Acosta, Spin orbifolds and the minimal genus problem, Dissertation, Tulane Uni-	24 25 26 27 28
	25 26 27 28 29	<ul> <li>Department, for hospitality.</li> <li><b>References</b></li> <li>[1] D. Acosta, <i>Spin orbifolds and the minimal genus problem</i>, Dissertation, Tulane University, 1997.</li> <li>[2] M. Ait Newle, <i>Computer and departs of terms hasts in Computer Vision</i>, 2010.</li> </ul>	24 25 26 27 28 29
	25 26 27 28 29 30	<ul> <li>Department, for hospitality.</li> <li><b>References</b></li> <li>[1] D. Acosta, <i>Spin orbifolds and the minimal genus problem</i>, Dissertation, Tulane University, 1997.</li> <li>[2] M. Ait Nouh, <i>Genera and degrees of torus knots in</i> CP<sup>2</sup>, J. Knot Theory Ramifications 18 (2009) no. 9, 1299–1312</li> </ul>	24 25 26 27 28 29 30
	25 26 27 28 29 30 31	<ul> <li>Department, for hospitality.</li> <li><b>References</b></li> <li>[1] D. Acosta, <i>Spin orbifolds and the minimal genus problem</i>, Dissertation, Tulane University, 1997.</li> <li>[2] M. Ait Nouh, <i>Genera and degrees of torus knots in</i> CP<sup>2</sup>, J. Knot Theory Ramifications 18 (2009), no. 9, 1299–1312.</li> <li>[3] Les neuds aui se dénouent par twist de Dehn dans la 3-sphère. Ph D thesis.</li> </ul>	24 25 26 27 28 29 30 31
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<uncited></uncited>	25 26 27 28 29 30 31 32 33 34	<ul> <li>Department, for hospitality.</li> <li><b>References</b></li> <li>[1] D. Acosta, <i>Spin orbifolds and the minimal genus problem</i>, Dissertation, Tulane University, 1997.</li> <li>[2] M. Ait Nouh, <i>Genera and degrees of torus knots in</i> CP<sup>2</sup>, J. Knot Theory Ramifications 18 (2009), no. 9, 1299–1312.</li> <li>[3], <i>Les nœuds qui se dénouent par twist de Dehn dans la 3-sphère</i>, Ph.D. thesis, University of Provence, Marseille, France, 2000.</li> <li>[4], <i>The minimal genus problem in</i> CP<sup>2</sup> # CP<sup>2</sup>, Algebr. Geom. Topol. 14 (2014), 671–686.</li> </ul>	24 25 26 27 28 29 30 31 32 33 34
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<uncited></uncited>	25 26 27 28 29 30 31 32 33 34 35 36	<ul> <li>Department, for hospitality.</li> <li><b>References</b></li> <li>[1] D. Acosta, <i>Spin orbifolds and the minimal genus problem</i>, Dissertation, Tulane University, 1997.</li> <li>[2] M. Ait Nouh, <i>Genera and degrees of torus knots in</i> CP<sup>2</sup>, J. Knot Theory Ramifications 18 (2009), no. 9, 1299–1312.</li> <li>[3], <i>Les nœuds qui se dénouent par twist de Dehn dans la 3-sphère</i>, Ph.D. thesis, University of Provence, Marseille, France, 2000.</li> <li>[4], <i>The minimal genus problem in</i> CP<sup>2</sup> # CP<sup>2</sup>, Algebr. Geom. Topol. 14 (2014), 671–686.</li> <li>[5] M. Ait Nouh and A. Yasuhara, <i>Torus knots that cannot be untied by twisting</i>, Rev. Mat. Complut. XIV (2001), no. 8, 423–437.</li> </ul>	24 25 26 27 28 29 30 31 32 33 34 35 36
<uncited></uncited>	25 26 27 28 29 30 31 32 33 34 35 36 37	<ul> <li>Department, for hospitality.</li> <li><b>References</b></li> <li>[1] D. Acosta, <i>Spin orbifolds and the minimal genus problem</i>, Dissertation, Tulane University, 1997.</li> <li>[2] M. Ait Nouh, <i>Genera and degrees of torus knots in</i> CP<sup>2</sup>, J. Knot Theory Ramifications 18 (2009), no. 9, 1299–1312.</li> <li>[3], <i>Les nœuds qui se dénouent par twist de Dehn dans la 3-sphère</i>, Ph.D. thesis, University of Provence, Marseille, France, 2000.</li> <li>[4], <i>The minimal genus problem in</i> CP<sup>2</sup> # CP<sup>2</sup>, Algebr. Geom. Topol. 14 (2014), 671–686.</li> <li>[5] M. Ait Nouh and A. Yasuhara, <i>Torus knots that cannot be untied by twisting</i>, Rev. Mat. Complut. XIV (2001), no. 8, 423–437.</li> <li>[6] D. Auckly, <i>Surgery, knots, and the Seiberg–Witten equations</i>, Lectures for the 1995</li> </ul>	24 25 26 27 28 29 30 31 32 33 34 35 36 37
<uncited></uncited>	25 26 27 28 29 30 31 32 33 34 35 36 37 38	<ul> <li>Department, for hospitality.</li> <li>References</li> <li>[1] D. Acosta, Spin orbifolds and the minimal genus problem, Dissertation, Tulane University, 1997.</li> <li>[2] M. Ait Nouh, Genera and degrees of torus knots in CP<sup>2</sup>, J. Knot Theory Ramifications 18 (2009), no. 9, 1299–1312.</li> <li>[3], Les nœuds qui se dénouent par twist de Dehn dans la 3-sphère, Ph.D. thesis, University of Provence, Marseille, France, 2000.</li> <li>[4], The minimal genus problem in CP<sup>2</sup> # CP<sup>2</sup>, Algebr. Geom. Topol. 14 (2014), 671–686.</li> <li>[5] M. Ait Nouh and A. Yasuhara, Torus knots that cannot be untied by twisting, Rev. Mat. Complut. XIV (2001), no. 8, 423–437.</li> <li>[6] D. Auckly, Surgery, knots, and the Seiberg–Witten equations, Lectures for the 1995 TGRCIW, preprint.</li> </ul>	24 25 26 27 28 29 30 31 32 33 34 35 36 37 38
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<uncited> <uncited> <uncited></uncited></uncited></uncited>	25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41	<ul> <li>Department, for hospitality.</li> <li><b>References</b></li> <li>[1] D. Acosta, <i>Spin orbifolds and the minimal genus problem</i>, Dissertation, Tulane University, 1997.</li> <li>[2] M. Ait Nouh, <i>Genera and degrees of torus knots in</i> CP<sup>2</sup>, J. Knot Theory Ramifications 18 (2009), no. 9, 1299–1312.</li> <li>[3], <i>Les nœuds qui se dénouent par twist de Dehn dans la 3-sphère</i>, Ph.D. thesis, University of Provence, Marseille, France, 2000.</li> <li>[4], <i>The minimal genus problem in</i> CP<sup>2</sup> # CP<sup>2</sup>, Algebr. Geom. Topol. 14 (2014), 671–686.</li> <li>[5] M. Ait Nouh and A. Yasuhara, <i>Torus knots that cannot be untied by twisting</i>, Rev. Mat. Complut. XIV (2001), no. 8, 423–437.</li> <li>[6] D. Auckly, <i>Surgery, knots, and the Seiberg–Witten equations</i>, Lectures for the 1995 TGRCIW, preprint.</li> <li>[7] T. Cochran and R. E. Gompf, <i>Applications of Donaldson's theorems to classical knot concordance, homology</i> 3-<i>sphere and property</i> P, Topology 27 (1988), 495–512.</li> <li>[8] M. Culler, C. M. Gordon, J. Luecke, and P. B. Shalen, <i>Dehn surgery on knots</i>, Ann. of Math, 125 (1987), 237–300.</li> </ul>	24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41
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<uncited> <uncited> <uncited></uncited></uncited></uncited>	25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44	<ul> <li>Department, for hospitality.</li> <li>References</li> <li>[1] D. Acosta, Spin orbifolds and the minimal genus problem, Dissertation, Tulane University, 1997.</li> <li>[2] M. Ait Nouh, Genera and degrees of torus knots in CP<sup>2</sup>, J. Knot Theory Ramifications 18 (2009), no. 9, 1299–1312.</li> <li>[3], Les næuds qui se dénouent par twist de Dehn dans la 3-sphère, Ph.D. thesis, University of Provence, Marseille, France, 2000.</li> <li>[4], The minimal genus problem in CP<sup>2</sup> # CP<sup>2</sup>, Algebr. Geom. Topol. 14 (2014), 671–686.</li> <li>[5] M. Ait Nouh and A. Yasuhara, Torus knots that cannot be untied by twisting, Rev. Mat. Complut. XIV (2001), no. 8, 423–437.</li> <li>[6] D. Auckly, Surgery, knots, and the Seiberg–Witten equations, Lectures for the 1995 TGRCIW, preprint.</li> <li>[7] T. Cochran and R. E. Gompf, Applications of Donaldson's theorems to classical knot concordance, homology 3-sphere and property P, Topology 27 (1988), 495–512.</li> <li>[8] M. Culler, C. M. Gordon, J. Luecke, and P. B. Shalen, Dehn surgery on knots, Ann. of Math. 125 (1987), 237–300.</li> <li>[9] R. Fox and J. Milnor, Singularities of 2-spheres in 4-space and cobordism of knots, Osaka J. Math. 3 (1966), 257–267.</li> <li>[10] P. Gilmer, Configurations of surfaces in 4-manifolds, Trans. Amer. Math. Soc. 264</li> </ul>	24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44
<uncited> <uncited> <uncited></uncited></uncited></uncited>	25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45	<ul> <li>Department, for hospitality.</li> <li>References</li> <li>[1] D. Acosta, Spin orbifolds and the minimal genus problem, Dissertation, Tulane University, 1997.</li> <li>[2] M. Ait Nouh, Genera and degrees of torus knots in CP<sup>2</sup>, J. Knot Theory Ramifications 18 (2009), no. 9, 1299–1312.</li> <li>[3], Les nœuds qui se dénouent par twist de Dehn dans la 3-sphère, Ph.D. thesis, University of Provence, Marseille, France, 2000.</li> <li>[4], The minimal genus problem in CP<sup>2</sup> # CP<sup>2</sup>, Algebr. Geom. Topol. 14 (2014), 671–686.</li> <li>[5] M. Ait Nouh and A. Yasuhara, Torus knots that cannot be untied by twisting, Rev. Mat. Complut. XIV (2001), no. 8, 423–437.</li> <li>[6] D. Auckly, Surgery, knots, and the Seiberg–Witten equations, Lectures for the 1995 TGRCIW, preprint.</li> <li>[7] T. Cochran and R. E. Gompf, Applications of Donaldson's theorems to classical knot concordance, homology 3-sphere and property P, Topology 27 (1988), 495–512.</li> <li>[8] M. Culler, C. M. Gordon, J. Luecke, and P. B. Shalen, Dehn surgery on knots, Ann. of Math. 125 (1987), 237–300.</li> <li>[9] R. Fox and J. Milnor, Singularities of 2-spheres in 4-space and cobordism of knots, Osaka J. Math. 3 (1966), 257–267.</li> <li>[10] P. Gilmer, Configurations of surfaces in 4-manifolds, Trans. Amer. Math. Soc. 264 (1981), 353–380.</li> </ul>	24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45

10

	1	[11] R. E. Gompf and A. I. Stipsicz, 4-Manifolds and Kirby calculus, Grad. Stud. Math.	1
	2	20, Amer. Math. Society, Providence, Rhode Island, 1999.	2
	3	[12] C. Goodman-Strauss, On composite twisted unknots, Trans. Amer. Math. Soc. 349 (1997) A429 A463	3
	4	[13] C. Hayashi and K. Motegi, Only single twisting on unknots can produce composite	4
	5	<i>knots</i> , Trans. Amer. Math. Soc. 349 (1997), no. 12, 4897–4930.	5
	6 7	[14] A. Kawauchi, A survey on knot theory, Birkhauser-Verlag, Basel-Boston-Berlin,	6 7
	/ 8	1996.	/ Q
	9	[15] R. C. Kirby, <i>The topology of 4-manifolds</i> , Lecture Notes in Math., Springer-Verlag, 1980	9
	10	[16] Y. Mathieu, Unknotting, knotting by twists on disks and property P for knots in $S^3$ ,	10
	11	Knots 90: proc. 1990 Osaka conf. on knot theory and related topics, pp. 93–102, de	11
	12	Gruyter, 1992.	12
	13	[17] J. Milnor and J. D. Stasheff, <i>Characteristic classes</i> , Princeton University Press, 1974.	13
	14	[18] K. Miyazaki and A. Yasuhara, <i>Knots that cannot be obtained from a trivial knot by</i>	14
	15	twisting, Contemp. Math. 164 (1994), 139–150.	15
	16	[19] T. Onyama, Twisting and unknowing operations, Rev. Mat. Only. Complet. Math. 7 (1994), 289–305.	16
	17	[20] R. Robertello, An Arf invariant of knot cobordism, Comm. Pure Appl. Math. 18	17
	18	(1965), 543–555.	18
	19	[21] A. Scorpan, The wild world of 4-manifolds, Amer. Math. Soc., Providence, Rhode	19
	20	Island, 2005.	20
	21	[22] M. Teragaito, <i>Composite knots trivialized by twisting</i> , J. Knot Theory Ramifications	21
	23	1 (1992), no. 4, 467-470.	23
	24	[25], Twisting operations and composite knois, FIGC. Affel: Math. Soc. 125 (1995) no 5 1623–1629	20
	25	[24] A. G. Tristram, <i>Some cobordism invariants for links</i> , Math. Proc. Cambridge Philos.	25
	26	Soc. 66 (1969), 251–264.	26
	27	[25] O. Y. Viro, Link types in codimension-2 with boundary, Uspekhi Mat. Nauk 30	27
	28	(1970), 231–232 (Russian).	28
<uncited></uncited>	29	[26] M. Yamamoto, <i>Lower bounds for the unknotting numbers of certain torus knots</i> , Proc.	29
runaitada	30	Amer. Math. Soc. 86 (1982), 519–524.	30
<unction <="" td=""><td>31</td><td>nected 4-manifolds Tokyo I Math 19 (1996) 245–261</td><td>31</td></unction>	31	nected 4-manifolds Tokyo I Math 19 (1996) 245–261	31
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5		······································	5
6	[1]	ACOSTA, D. J. (1997). Spin orbifolds and the minimal genus problem. ProQuest LLC,	6
7		Ann Arbor, MI. Thesis (Ph.D.)–Tulane University. MR2696868	7
8	[2]	NOUH, M. A. (2009). Genera and degrees of torus knots in CP <sup>2</sup> . J. Knot Theory	8
9	[2]	Ramifications 18 1299–1312. DOI:10.1142/S021821650900/439 MR2569563	9
10	[3]	Not Found! Narry M. A. (2014). The minimul energy multiplication in $\mathbb{C}\mathbb{D}^2 \# \mathbb{C}\mathbb{D}^2$ . Also, by $\mathbb{C}$ and	10
11	[4]	<i>Topol.</i> <b>14</b> 671–686. DOI:10.2140/agt.2014.14.671 MR3159966	11
12	[5]	AIT NOUH, M. AND YASUHARA, A. (2001). Torus knots that cannot be untied by	12
13		twisting. Rev. Mat. Complut. 14 423-437. MR1871306	13
14	[6]	Not Found!	14
15	[7]	COCHRAN, T. D. AND GOMPF, R. E. (1988). Applications of Donaldson's theorems	15
16		to classical knot concordance, homology 3-spheres and property P. Topology 27	16
17		495–512. DOI:10.1016/0040-9383(88)90028-6 MR0976591	17
18	[8]	CULLER, M., GORDON, C. M., LUECKE, J., AND SHALEN, P. B. (1987). Dehn surgery	18
19	503	on knots. Ann. of Math. (2) <b>125</b> 237–300. DOI:10.2307/1971311 MR0881270	19
20	[9]	Fox, R. H. AND MILNOR, J. W. (1966). Singularities of 2-spheres in 4-space and	20
21	[10]	CONSTRUCT D M (1081) Conformation of surfaces in A manifolds. Turne Amon Math	21
22	[10]	GILMER, P. M. (1981). Configurations of surfaces in 4-manifolds. <i>Trans. Amer. Math.</i>	22
23	[11]	GONDE P. E. AND STIDERZ A. I. (1000). A manifolds and Kirby calculus Gradu	23
24	[11]	ate Studies in Mathematics Vol <b>20</b> American Mathematical Society Providence	24
25		RI DOI:10.1090/gsm/020_MR1707327	25
26	[12]	GOODMAN-STRAUSS, C. (1997). On composite twisted unknots. Trans. Amer. Math.	26
27	[]	Soc. <b>349</b> 4429–4463. DOI:10.1090/S0002-9947-97-01627-9 MR1355072	27
28	[13]	HAYASHI, C. AND MOTEGI, K. (1997). Dehn surgery on knots in solid	28
29		tori creating essential annuli. Trans. Amer. Math. Soc. 349 4897–	29
30	51.43	4930. DOI:10.1090/S0002-9947-97-01723-6 MR1373637	30
31	[14]	KAWAUCHI, A. (1996). A survey of knot theory. Birkhauser Verlag, Basel. Iranslated	31
32	[15]	and revised from the 1990 Japanese original by the author. $MR141/494$	32
33	[13]	Val <b>1374</b> Springer Verlag Parlin MP1001066	33
34	[16]	MATHIEL V (1902) Unknotting knotting by twists on disks and property (P) for	34
35	[10]	knots in $S^3$ In <i>Knots</i> 90 ( <i>Osaka</i> 1990) de Gruvter Berlin 93–102 MR1177414	35
36	[17]	MUNOR I W AND STASHFFF I D (1974) Characteristic classes Princeton Univer-	36
37	[1,]	sity Press, Princeton, N. J.: University of Tokyo Press, Tokyo, Annals of Mathematics	37
38		Studies, No. 76. MR0440554	38
39	[18]	MIYAZAKI, K. AND YASUHARA, A. (1994). Knots that cannot be ob-	39
40		tained from a trivial knot by twisting. In Geometric topology (Haifa,	40
41		1992). Contemp. Math., Vol. 164. Amer. Math. Soc., Providence, RI, 139-	41
12		150. DOI:10.1090/conm/164/01590 MR1282760	42
12	[19]	OHYAMA, Y. (1994). Twisting and unknotting operations. Rev. Mat. Univ. Complut.	42
40		Madrid 7 289–305. MR1297516	43
-1-1 / E	[20]	ROBERTELLO, R. A. (1965). An invariant of knot cobordism. Comm. Pure Appl.	44
40		Math. 18 543–555. MR0182965	45
40			46

1	[21]	SCORPAN, A. (2005). The wild world of 4-manifolds. American Mathematical Society,	1
2		Providence, RI. MR2136212	2
3	[22]	TERAGAITO, M. (1995). Twisting operations and composite knots. Proc. Amer. Math.	3
4		Soc. 123 1623-1629. DOI:10.2307/2161156 MR1254855	4
5	[23]	TERAGAITO, M. (1992). Composite knots trivialized by twisting. J. Knot Theory	5
6		Ramifications 1 467-470. DOI:10.1142/S0218216592000239 MR1194998	6
7	[24]	TRISTRAM, A. G. (1969). Some cobordism invariants for links. Proc. Cambridge	7
8		Philos. Soc. 66 251–264. MR0248854	8
9	[25]	Not Found!	9
10	[26]	YAMAMOTO, M. (1982). Lower bounds for the unknotting numbers of certain torus	10
11	[27]	Knols. Proc. Amer. Math. Soc. <b>80</b> 519–524. DOI:10.250//2044401 MR00/1228	11
12	[27]	and representing formation of the second sec	12
13		261 DOI:10.3836/tim/1270043232 MR1391941	13
14		201. D01.10.5050kglin 1270015252 (MR1591)11	14
15			15
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