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Calc II

76 Suppose  $\int_0^2 g(t) dt = 5$  Calculate the following

a)  $\int_0^4 g(t/2) dt$

$$\int_0^4 g\left(\frac{t}{2}\right) dt$$

$$w = t/2 \\ dw = 1/2 dt \\ dt = 2dw$$

$$4, \left(\frac{4}{2}\right) = 2 \quad 0, \frac{0}{2} = 0$$

$$2 \int_0^2 g(t) dt = 2(5) = 10$$

b)  $\int_0^2 g(2-t) dt$

$$\int_0^2 g(2-t) dt$$

$$w = 2-t \\ dw = -1 dt \\ dt = -dw$$

$$2, (2-2) = 0 \quad 0, (2-0) = 2$$

$$\int_0^2 g(t) dw + 1 = 1 \int_0^2 g(t) dt = 5$$

$$1(5) = 5$$

78  $\int_{-\pi}^{\pi} \cos^2 \theta \sin \theta d\theta$

a)  $\int_{-\pi}^{\pi} \cos^2 \theta \sin \theta d\theta$

$$\int_{-\pi}^{\pi} \cos \theta \cdot \cos \theta \cdot \sin \theta d\theta$$

$$u = \cos \theta \\ du = -\sin \theta d\theta$$

$$= \int u^2 du = -\left[\frac{u^3}{3}\right] = -\frac{\cos^3 \theta}{3} \Big|_{-\pi}^{\pi} \\ = -\frac{\cos^3 \theta}{3} + C$$

b)  $= -\frac{\cos^3 \theta}{3} \Big|_0^{\pi}$

$$= \frac{-(\cos(\pi))^3}{3} - \left[ \frac{-(\cos(0))^3}{3} \right]$$

$$= -\frac{(-1)^3}{3} - \left( \frac{-(1)^3}{3} \right)$$

$$= \frac{1}{3} + \frac{1}{3} = \frac{2}{3}$$

$$= \frac{-(-1)^3}{3} - \left( \frac{-(-1)^3}{3} \right) = \frac{-(\cos(\pi))^3}{3} - \left[ \frac{-(\cos(-\pi))^3}{3} \right]$$

$$= \frac{1}{3} - \frac{1}{3} = 0$$

norma

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$$\int e^x \sin x \, dx \quad \int u v' \, dx = uv - \int u' v \, dx$$

$$u = e^x \quad u' = e^x$$

$$v' = \sin x \quad v = -\cos x$$

$$I_1 = e^x - \cos x - \int e^x - \cos x \, dx = I_2$$

↳

$$u = e^x \quad u' = e^x$$

$$v' = -\cos v = -\sin x$$

$$I_2 = -e^x \sin x - \int -e^x \sin x$$

$$I_2 = -e^x \sin x + \int e^x \sin x$$

$$I_1 = e^x - \cos x - [-e^x \sin x + \int e^x \sin x]$$

$$2I_1 = e^x - \cos x + e^x \sin x$$

$$I_1 = \frac{1}{2} e^x - \cos x + e^x \sin x + C \quad \boxed{A = I_1 = \frac{1}{2} e^x (-\cos x + \sin x) + C}$$

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$$\int x^n e^x \, dx = x^n e^x - n \int x^{n-1} e^x \, dx$$

↳

$$A = \boxed{\begin{matrix} u = x^n & u' = nx^{n-1} \\ v' = e^x & v = e^x \end{matrix}}$$