

3. Suppose we use Gauss elimination to solve an N by N linear system, and distribute the columns by "blocks" over the processors: each processor stores the entire matrix, but the first $NB=N/NPES$ columns are only touched by processor 0, the second NB columns by processor 1, etc. How would you modify the innermost loop of DLINEQ, shown below:

```
      DO 25 K=I,N
          A(J,K) = A(J,K) - LJI*A(I,K)
25     CONTINUE
```

Use ITASK for the processor number, and NPES for the number of processors, and assume N is divisible by NPES. Hint: the limits are simpler now than when the columns are distributed cyclically, and remember that if $I1 > I2$, no trips through a loop "DO K=I1,I2" will be made.

4. What is the output from the MPI Fortran program below, if run on NPES=3 processors?

```
      PARAMETER (N=12)
      DOUBLE PRECISION X(N),SUMI,SUM
      INCLUDE 'mpif.h'
C           INITIALIZE MPI
      CALL MPI_INIT (IERR)
C           NPES = NUMBER OF PROCESSORS
      CALL MPI_COMM_SIZE (MPI_COMM_WORLD, NPES, IERR)
C           ITASK = MY PROCESSOR NUMBER
      CALL MPI_COMM_RANK (MPI_COMM_WORLD, ITASK, IERR)
```

```

DO I=1,N
  IF (MOD(I-1, NPES).EQ.ITASK) THEN
    X(I) = I
  ENDIF
ENDDO
C
SUMI = 0
DO I=ITASK+1,N, NPES
  SUMI = SUMI + X(I)
ENDDO
iroot = 1
CALL MPI_REDUCE(SUMI, SUM, 1, MPI_DOUBLE_PRECISION,
&               MPI_SUM, iroot, MPI_COMM_WORLD, IERR)
if (ITASK.EQ.iroot) PRINT *, SUMI, SUM
CALL MPI_FINALIZE(IERR)
STOP
END

```

5. In deriving the Black-Scholes partial differential equation, we assumed what type of probability distribution for the price S at future time $=T$ of an asset whose price is s at time $=t$? What did we assume for the mean and the standard deviation of this distribution? The asset volatility is σ_1 , the strike price is E and the risk-free interest rate (rate of inflation, sort of) is r .

