

- 1) Your college newspaper, *The Collegiate Investigator*, has fixed production costs of \$70 per edition and marginal printing and distribution costs of 40¢ per copy. *The Collegiate Investigator* sells for 50¢ per copy.
 - a) Write down the associated cost, revenue, and profit functions.
 - b) What profit (or loss) results from the sale of 500 copies of *The Collegiate Investigator*?
 - c) How many copies should be sold in order to break even?

- 2) Let $f(x) = x^2 + 3x + 1$
 - a) $f(0)$
 - b) $f(-1)$
 - c) $f(a)$
 - d) $f(x + h)$, simplify.

- 3) Find the equation of the line that passes through the points $(-2, 1)$ and $(2, 3)$.

- 4) The XYZ Widget factory can produce 80 widgets in a day at a total cost of \$8,000 and it can produce 100 widgets a day at a total cost of \$10,000.
 - a) What are the company's daily fixed costs and marginal cost per widget?
 - b) Use the cost function to estimate the cost of manufacturing 400 widgets in a day.

- 5) You can sell 100 pet rocks per week if they are marked at \$1 each, but only 40 each week if they are marked at \$2 per rock. Your rock supplier is prepared to sell you 30 rocks each week if they are marked at \$1/rock, and 120 each week if they are marked at \$2 per rock.
 - a) Write down the associated linear demand and supply functions.
 - b) At what price should the rocks be marked so that there is neither a surplus nor a shortage of rocks?

- 6) The following table shows worldwide sales of a certain type of cell phones and their average wholesale process in 2014 and 2018.

Year	2014	2018
Selling Price (\$)	325	245
Sales (millions)	1,110	1,910

- a) Use the data to obtain a linear demand function for this type of cell phones.

$$q(p) =$$

- b) Use your demand equation to predict sales to the nearest million phones if the price is raised to \$375.
- c) Fill in the blanks: For every \$1 increase in price, sales of cell phones decrease by _____ units.
- 7) Sketch the graph of the quadratic function, indicating the coordinates of the vertex, the y -intercept, and the x -intercepts (if any).

$$f(x) = -x^2 + 4x - 4$$

- 8) The Better Baby Buggy Co. has just come out with a new model, the Turbo. The market research department predicts that the demand equation for Turbos is given by

$$q = -4p + 480,$$

where q is the number of buggies the company can sell in a month if the price is $\$p$ per buggy.

- a) At what price should it sell the buggies to get the largest revenue?
- b) What is the largest monthly revenue?

- 9) Actinium is a highly radioactive element. The most common isotope of actinium is produced as a by-product in nuclear reactors, and has a half-life of 21.77 years.

- a) Obtain an exponential decay model for actinium-227 in the form $Q(t) = Q_0 e^{-kt}$. (Round k to four decimal places.)
- b) About 20 milligrams of actinium are produced in a certain nuclear reactor. Use your model to predict how long it will take for this amount of actinium to decay to one milligram.

10) The half-life of cobalt 60 is 5 years.

- a) Obtain an exponential model for cobalt 60 in the form $Q(t) = Q_0e^{-kt}$. (Round coefficients to three significant digits.)
- b) Use your model to predict, to the nearest year, the time it takes for one third of the sample of cobalt 60 to decay.

11) The rate of auto thefts **triples** every 9 months.

- a) Determine, to two decimal places, the base b for an exponential model $y = Ab^t$ of the rate of auto thefts as a function of time in months.
 $b =$
- b) Find the doubling time to the nearest tenth of a month.

12) There were 3,500 bacteria in a Petri dish (at time $t = 0$ hours). Four hours later, there were 5,500 bacteria in the dish. Find the mathematical model that represents the number of bacteria after t hours. It's an exponential formula of the form $Q(t) = Q_0e^{kt}$.

Round k to 4 decimal places. Include the units in the answer.