

1D Steady-State Problems (Galerkin method)

ODEs:

$$\begin{aligned} \frac{\partial}{\partial x} A_1(x, U_1, U_{1x}, \dots, U_N, U_{Nx}) &= F_1(x, U_1, U_{1x}, \dots, U_N, U_{Nx}) \\ &\cdot \quad \quad \quad = \quad \quad \cdot \\ &\cdot \quad \quad \quad = \quad \quad \cdot \\ \frac{\partial}{\partial x} A_N(x, U_1, U_{1x}, \dots, U_N, U_{Nx}) &= F_N(x, U_1, U_{1x}, \dots, U_N, U_{Nx}) \end{aligned}$$

Boundary conditions (at endpoints):

$$\begin{aligned} U_1 &= FB_1 \\ &\cdot \quad = \quad \cdot \\ &\cdot \quad = \quad \cdot \\ UN &= FB_N \end{aligned}$$

or ($N_x = -1$ at left end, $+1$ at right end)

$$\begin{aligned} A_1 N_x &= GB_1(U_1, U_{1x}, \dots, U_N, U_{Nx}) \\ &\cdot \quad = \quad \cdot \\ &\cdot \quad = \quad \cdot \\ A_N N_x &= GB_N(U_1, U_{1x}, \dots, U_N, U_{Nx}) \end{aligned}$$