

## Multiplying and Dividing Rational Expressions – Intermediate Algebra

To Multiply Rational Expressions:

1. Factor the numerator and denominator of each fraction (if possible).
- ~~X~~ 2. Divide out any common factors.
- ~~X~~ 3. Rewrite as a single fraction.
4. Leave in factored form.

Examples: Multiply the rational expressions.

$$1. \frac{40x^3}{6y} \cdot \frac{15y^2}{5x^5} = \frac{\cancel{5} \cdot \cancel{8} x^3}{\cancel{2} \cdot \cancel{3} y} \cdot \frac{\cancel{3} \cdot \cancel{5} y^2}{\cancel{5} x^5} = \frac{4 \cdot 5 x^3}{y x^5} = \boxed{\frac{20y}{x^2}}$$

$$\begin{aligned} 40 &= 5 \cdot 8 \\ 15 &= 3 \cdot 5 \\ 6 &= 2 \cdot 3 \\ 5 &= \end{aligned}$$

$$2. \frac{a+5}{a-2} \cdot \frac{a-3}{a+4} = \boxed{\frac{(a+5)(a-3)}{(a-2)(a+4)}}$$

$$3. \frac{(h+2)(h-8)}{(h-8)(h-6)} \cdot \frac{(h-6)(h+3)}{(h-2)(h-7)} = \boxed{\frac{(h+2)(h+3)}{(h-2)(h-7)}}$$

$$4. \frac{n^2 + 6n + 8}{n^2 + 3n + 2} \cdot \frac{n^2 - 1}{n^2 + 8n + 16} = \frac{\cancel{(n+4)(n+2)}}{\cancel{(n+1)(n+1)}} \cdot \frac{\cancel{(n+1)(n-1)}}{\cancel{(n+4)(n+4)}} = \frac{n-1}{n+4}$$

$$n^2 + 6n + 8 = (n + 4)(n + 2)$$

$$n^2 - 1 = (n + 1)(n - 1)$$

$$n^2 + 3n + 2 = (n + 2)(n + 1)$$

$$n^2 + 8n + 16 = (n + 4)(n + 4)$$

To Divide Rational Expressions:

1. Multiply by the reciprocal of the second fraction.
2. Factor the numerator and denominator of each fraction (if possible).
3. Divide out any common factors.
4. Rewrite as a single fraction.
5. Leave in factored form.

$$\frac{\frac{1}{2}}{\frac{3}{4}} \cdot \frac{\frac{4}{3}}{\frac{4}{3}} = \frac{\frac{1}{2} \cdot \frac{4}{3}}{1}$$

Examples: Divide the following rational expressions.

$$1. \frac{8}{15} \div \frac{4}{7} = \frac{8}{15} \cdot \frac{7}{4}$$

$$= \frac{14}{15}$$

$$2. \frac{d+3}{d-5} \div \frac{d+3}{d+8} = \frac{d+3}{d-5} \cdot \frac{d+8}{d+3} = \frac{(d+3)(d+8)}{(d-5)(d+3)} = \frac{d+8}{d-5}$$

$$3. \frac{18x^2 + 9x - 20}{x^2 + 2x - 35} \div \frac{6x^2 + 13x - 15}{x^2 + 10x + 21} = \frac{\cancel{(6x-5)(3x+4)}}{\cancel{(x+7)(x-5)}} \cdot \frac{\cancel{(x+7)(x+3)}}{\cancel{(6x-5)(x+3)}} = \boxed{\frac{3x+4}{x-5}}$$

$$x^2 + 2x - 35 = (x+7)(x-5)$$

$$x^2 + 10x + 21 = (x+7)(x+3)$$

$$6x^2 + 13x - 15 = \underbrace{6x^2 - 5x}_{x(6x-5)} + 18x - 15 + 3(6x-5) \\ (6x-5)(x+3)$$

$$(6 \cdot -15) = -90 \quad \begin{array}{r} \cancel{-15} \\ \hline -6 \end{array} \quad \begin{array}{r} \cancel{-15} \\ \hline -5 \end{array}$$

*guess!*

$$18x^2 + 9x - 20 = (6x-5)(3x+4)$$

$$18(-20) =$$

$$\text{check: } 18x^2 + 24x - 15x - 20$$

$$18x^2 + 9x - 20 \checkmark$$